- 14. (a) Given  $\frac{dy}{dx} = \left(\frac{1}{2}\right)\left(1+x^2\right)y^2$  and y(0) = 1, y(0.1) = 1.06, y(0.2) = 1.12, y(0.3) = 1.21, evaluate y(0.4) by Milne's predictor-Corrector Method correct to 4 decimal places. (10)
  - (ii) Solve the equation  $\frac{dy}{dx} = 1 y$ , y(0) = 0 using modified Euler's method and tabulate the solutions at x = 0.1 and 0.2 correct to 4 decimal places. (6)

Or

(b) Given 
$$\frac{dy}{dx} = y - x^2 + 1$$
,  $y(0) = 0.5$ . (16)

- (i) Using the modified Euler's method, find y(0.2)
- (ii) Using the 4<sup>th</sup> order Runge-Kutta method, find y(0.4) and y(0.6).
- (iii) Using Adams-Bash forth Predictor-Corrector Method, find y(0.8).
- 15. (a) Solve  $2u_t = u_{xx}$ , u(0,t) = 0, u(4,t) = 0, u(x,0) = x(4-x) with h = 1. Find the values of u upto t = 5. (16)

Or

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(b) Find the model values of the wave equation  $\frac{\partial^2 u}{\partial t^2} = 16 \frac{\partial^2 u}{\partial x^2}$  given that u(0,t) = u(5,t) = 0,  $u(x,0) = x^2(5-x)$  and  $u_t(x,0) = 0$  taking h = 1 and upto one half of the period of vibration.

Reg. No.:						

# Question Paper Code: 50838

## B.E./B.Tech. DEGREE EXAMINATIONS, APRIL/MAY 2023.

### Fourth/Fifth/Sixth Semester

#### Civil Engineering

#### MA 8491 - NUMERICAL METHODS

(Common to: Aeronautical Engineering/Aerospace Engineering/
Agriculture Engineering/Electrical and Electronics Engineering/Electronics and
Instrumentation Engineering/Instrumentation and Control
Engineering/Manufacturing Engineering/Mechanical Engineering
(Sandwich)/Mechanical and Automation Engineering/Biotechnology and
Biochemical Engineering/Chemical Engineering/Chemical and Electrochemical
Engineering/Plastic Technology/Polymer Technology/Textile technology)

(Regulations 2017)

Time: Three hours

Maximum: 100 marks

#### Answer ALL questions.

PART A — 
$$(10 \times 2 = 20 \text{ marks})$$

- 1. What is the First iteration approximate solution of the equation 4x + y = 8 and 2x + 3y = 7 solved by Gauss Jacobi Method?
- 2. Find all eigen values of the matrix A by Jacobi's method where  $A = \begin{pmatrix} 2 & -3 \\ -3 & 2 \end{pmatrix}$ .
- 3. Form the divided difference table for the following data:

- 4. Find the Lagrange's interpolating polynomial passing through the points (0,0)(1,1)(2,20).
- 5. Evaluate  $\int_{-1}^{1} \frac{dx}{1+x^2}$  by using two-point Gaussian quadrature formula.

6. Find  $\frac{dy}{dx}$  of x = 50 by using the following Forward difference

$$x \quad y \quad \Delta y \quad \Delta^2 y$$

- 52 3.7325
- 7. Using Euler's method, find y at x = 0.1 if  $\frac{dy}{dx} = 1 + xy$ , y(0) = 2.
- 8. State the Milne's predictor and corrector formula for solving differential equation numerically.
- 9. Write the finite difference scheme for  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 y}{\partial y^2} = 8x^2y^2$  for a square region with mesh size  $\Delta x = \Delta y = 1$ .
- 10. Write the explicit formula for one-dimensional wave equation if  $1 \lambda^2 \alpha^2 = 0$  and  $\lambda = \frac{k}{h}$ .

PART B — 
$$(5 \times 16 = 80 \text{ marks})$$

- 11. (a) (i) Find a real root of the equation  $\cos x = 3x 1$  correct to three decimal places by iteration method. (6)
  - (ii) Find the largest Eigen value and its corresponding Eigen vector of

the matrix 
$$A = \begin{pmatrix} 1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 \end{pmatrix}$$
 by power method Take  $X_0 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$ . (10)

Or

(b) Solve the following system of equations by Gauss-Seidal Method (16)

$$20x + y - 2z = 17$$

$$3x + 20y - z = -18$$

$$2x - 3y + 20z = 25$$

12. (a) (i) Use Newton's backward difference formula to construct an interpolating polynomial of degree 3 for the data: (10)

$$x: -0.75 -0.5 -0.25$$

f(x): -0.07181250 0.024750 0.33493750 1.10100

(ii) In the following table, the values of y are consecutive terms of a series of which 23.6 is the 6th term. Find the first term of the series.

y: 4.8 8.4 14.5 23.6 36.2 52.8 73.9

Or

(b) Using the following table values, find the natural cubic spline approximation are hence evaluate the value of y at x = 2.5. (16)

$$x: 0 1 2 3$$
  
 $y: 1 2 33 244$ 

13. (a) (i) Using the approximate Newton's Interpolation formula to find  $\frac{dy}{dx} \text{ and } \frac{d^2y}{dx^2} \text{ at } x = 2.2 \text{ from the following data:} \tag{10}$ 

(ii) Use Gaussian quadrature three points formula to evaluate the integral  $\int_{-x}^{2} \frac{dx}{x}$ . (6)

Or

- (b) Consider the following data:
  - x: 0 0.125 0.250 0.375 0.50 0.675 0.750 0.875 1  $y = \frac{1}{1+x^2}:$  1 0.9846 0.9412 0.8767 0.8 0.7191 0.64 0.5664 0.5

with 
$$h = 0.5, 0.25, 0.125$$
 and use Romberg's method to compute 
$$\int_{0}^{1} \frac{1}{1+x^{2}} dx$$
. Hence deduce an approximate value of  $\pi$ . (16)