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Reg. No.:

Question Paper Code: 23768

B.E./B.Tech. DEGREE EXAMINATION, NOVEMBER/DECEMBER 2018.

Third/Fifth Semester

Civil Engineering

MA 2211 — TRANSFORMS AND PARTIAL DIFFERENTIAL EQUATIONS

(Common to all branches)

(Regulations 2008)

Time: Three hours

Maximum: 100 marks

Answer ALL questions,

PART A —
$$(10 \times 2 = 20 \text{ marks})$$

- 1. If $f(x) = x^2$ in -2 < x < 2 and f(x+4) = f(x), then find the coefficient a_0 of its Fourier series.
- 2. Find the root mean square value of $f(x) = \cos x$ in $(0, 2\pi)$.
- 3. State the convolution theorem for Fourier transform.
- 4. Show that the Fourier transform satisfies the linearity property.
- 5. Form the partial differential equation by eliminating the arbitrary function from $z = f(x^2 + y^2)$.
- 6. Find the complete integral of p = 2qx.
- 7. Mathematically formulate the following vibrating string problem: "A string is stretched between two fixed points at a distance 2l apart and the points of the string are given an initial velocity f(x), x being the distance from an end point".
- 8. Classify the partial differential equation: $u_{xx} + 2u_{xy} + u_{yy} = 0$.
- 9. Find the Z transform of u(n-1).
- 10. State the initial value theorem of Z transform.

PART B — $(5 \times 16 = 80 \text{ mark})$	$(5 \times 16 = 80 \text{ mark})$	= 80	16 =	X	(5)	B (B	RT	PA
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- 11. (a) (i) Find a Fourier series to represent $f(x) = x x^2$ from $-\pi$ to π . (10)
 - (ii) Obtain the constant term a_0 and the first two harmonics a_1 and a_2 in the Fourier cosine series representation of y = f(x) in (0, 6) for the given table of values:

x 0 1 2 3 4 5

y 4 8 15 7 6 2

Or

(b) (i) Find the half range Fourier sine series expansion for

$$f(x) = \begin{cases} \frac{2kx}{L}, & 0 < x < L/2 \\ \frac{2k(L-x)}{L}, & L/2 < x < L \end{cases}$$
. Hence evaluate $\sum_{n=1}^{\infty} \frac{1}{(2n-1)^4}$. (8)

- (ii) Find the complex form of the Fourier series for $f(x) = e^{-x}$, -1 < x < 1.
- 12. (a) (i) Express the function $f(x) = \begin{cases} 1, & |x| \le 1 \\ 0, & |x| > 1 \end{cases}$ as a Fourier integral.

 Hence evaluate $\int_0^\infty \frac{\sin \lambda}{\lambda} d\lambda$. (10)
 - (ii) Find the Fourier sine transform of $\frac{1}{x}$. (6)

Or

- (b) (i) Find the Fourier transform of $e^{-a^2x^2}$, a>0 and hence find the Fourier transform of $e^{-x^2/2}$. (8)
 - (ii) Using Fourier transform methods, evaluate $\int_{0}^{\infty} \frac{dx}{(x^{2} + a^{2})(x^{2} + b^{2})}, a, b > 0.$ (8)
- 13. (a) (i) Solve the partial differential equation: $z^2(p^2+q^2)=x^2+y^2$. (8)
 - (ii) Solve $(D^2 + 2DD' + D'^2)z = \sinh(x + y) + e^{x+2y}$. (8)

Or

- (b) (i) Solve (3z-4y)p+(4x-2z)q=2y-3x. (8)
 - (ii) Obtain the complete solution and singular solution of $z = px + qy + p^2q^2$. (8)

14. (a) A rod, 30 cm long, has its ends A and B kept at 20°C and 80°C respectively until steady state conditions prevail. The temperature at each end is then suddenly reduced to 0°C and kept so. Find the resulting temperature function u(x, t) taking x = 0 at A. (16)

Or

- (b) An infinitely long plane uniform plate is bounded by two parallel edges x = 0 and x = l and an edge at right angles to them. The breadth of this edge y = 0 is l and is maintained at a temperature f(x). All the other three edges are at zero temperature. Find the steady state temperature at any interior point of the plate. (16)
- 15. (a) (i) Using Z-transform method, solve the difference equation: x(n+1)-2x(n)=1 given x(0)=0. (10)
 - (ii) Find the Z transform of t^k and hence deduce the result: $Z(t^k) = -Tz \frac{d}{dz} \{Z(t^{k-1})\}$, where T is the sampling period with t = nT, n = 0, 1, 2, ...

Or

- (b) (i) Find the inverse Z transform of $\frac{z^2}{\left(z-\frac{1}{2}\right)\left(z-\frac{1}{4}\right)}$ using partial fractions method.
 - (ii) Find the inverse Z transform $\frac{z^2}{(z-a)^2}$ using convolution theorem.