

PART B — (5 × 13 = 65 marks)

11. (a) Write the differential equations governing the behavior of the translational mechanical systems shown in Figure 1 and hence find $X_1(s)$. (13)

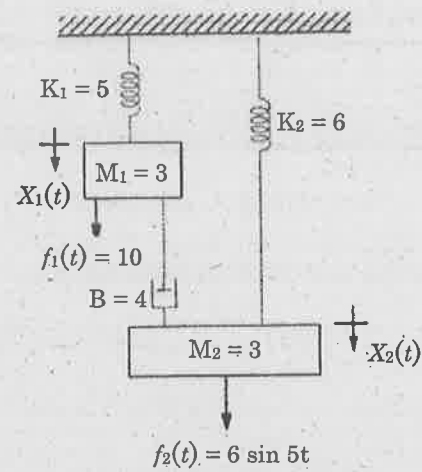


Figure 1
Or

- (b) A system is represented by signal flow graph shown in Figure 2, obtain the overall gain of the system using Mason's gain formula. (13)

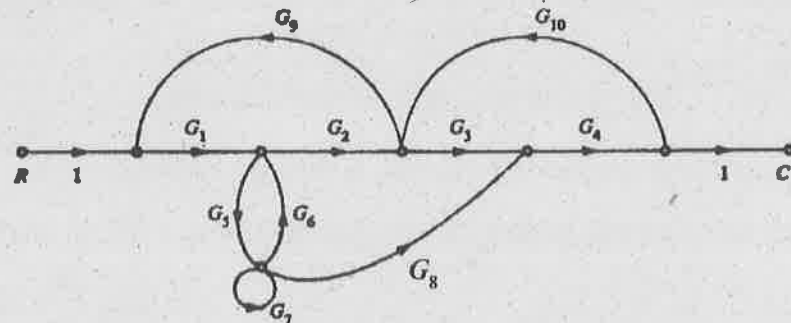


Figure 2

12. (a) (i) Consider the system shown in Figure 3, where damping ratio is 0.6 and natural undamped frequency is 5 rad/sec. Obtain the rise time t_r , peak time t_p , maximum overshoot M_p , and settling time 2% and 5% criterion t_s when the system is subjected to a unit-step input. (6)

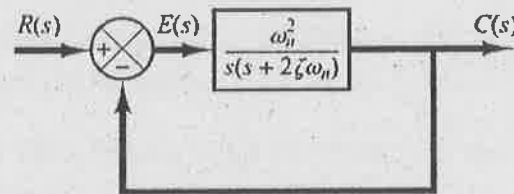


Figure 3

- (ii) Derive the expression for peak time and settling time for the underdamped second order system with unit step input. (7)

Or

- (b) (i) For a unity feedback system $G(s) = \frac{200}{s(s+8)}$ and $r(t) = 2t$ determine steady state error. If it is desired to reduce this existing error by 5% find the new gain of the system. (7)

- (ii) Explain in detail about PID controllers used in control systems. (6)

13. (a) The open loop transfer function with unity feedback given by $G(s) = \frac{1}{s(1+0.1s)(1+s)}$. From the bode plot, determine the gain crossover frequency, phase crossover frequency, gain margin and phase margin. (13)

Or

- (b) The open loop transfer function for a unity feedback system is given by, $G(S) = \frac{K}{S(1+0.2S)(1+0.05S)}$. Sketch the polar plot and determine the value of K so that gain margin is 18dB. (13)

14. (a) Sketch the root locus of the system whose transfer function is given by $\frac{C(s)}{R(s)} = \frac{K}{s(s+4)(s^2+s+1)+K}$. (13)

Or

- (b) Sketch the Nyquist plot for the following open loop transfer function is given by $G(s)H(s) = \frac{K(1+s)^2}{s^3}$. Determine the range of K for stability. (13)

15. (a) A system is given by

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 2 \end{bmatrix} [u] \text{ with } \begin{bmatrix} x_1(0) \\ x_2(0) \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

Where u is unit step function. Find the state transition matrix and there from find the state response, i.e.. $x(t)$ for $t > 0$. (13)

Or

- (b) Find the state equation and output equation for the system given by $\frac{Y(s)}{R(s)} = \frac{s^3 + 5s^2 + 6s + 1}{s^3 + 4s^2 + 3s + 3}$. Also check for controllability and observability. (13)